Lecture 6b Introduction to Public Key Cryptography

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version 1.0

Plan



- 1. Public key cryptography an overview
- 2. The key management problem
 - 1. qualified signatures
 - 2. public key infrastructure
- 3. Identity-based cryptography

Public-Key Cryptography

also called: asymmetric cryptography



Ralph Merkle (1974)

Whitfield Diffie and Martin Hellman (1976)

A little bit of history

Diffie and Hellman were the first to publish a paper containing the idea of the public-key cryptography:

W.Diffie and M.E.Hellman, New directions in cryptography IEEE Trans. Inform. Theory, IT-22, 6, 1976, pp.644-654.

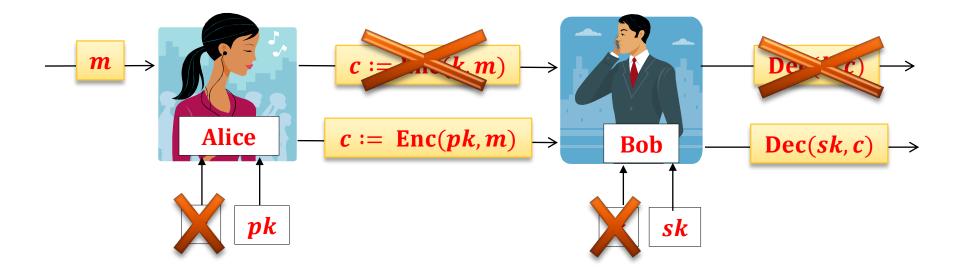
A similar idea was described by **Ralph Merkle**: in **1974** he described it in a project proposal for a Computer Security course at UC Berkeley (it was rejected) in **1975** he submitted it to the CACM journal (it was rejected) (see <u>www.merkle.com/1974/</u>)

In **1997** the GCHQ (the British equivalent of the NSA) revealed that they knew it already in **1973**.

The idea

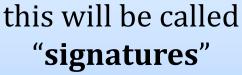
Instead of using one key *k*, use 2 keys (*pk*, *sk*), where *pk* is used for encryption, *sk* is used for decryption. pk can be public, and only sk has to be kept secret!

That's why it's called: **public-key cryptography**

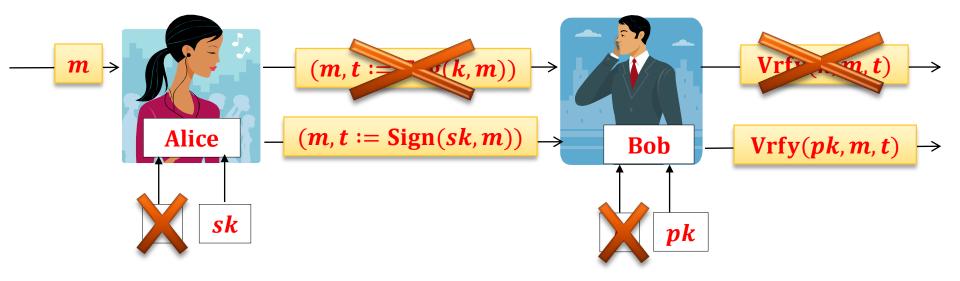


The same thing works for authentication

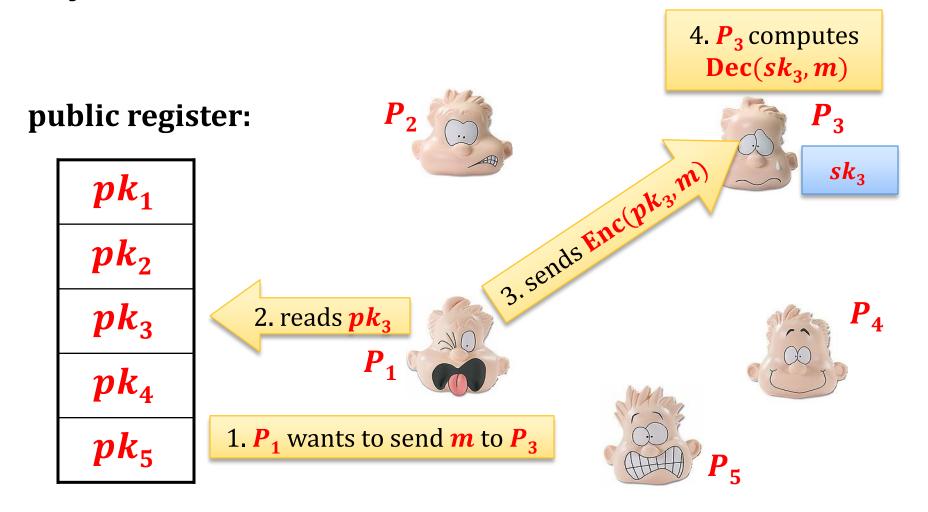
- *sk* is used for computing a tag,
- *pk* is used for verifying correctness of the tag.



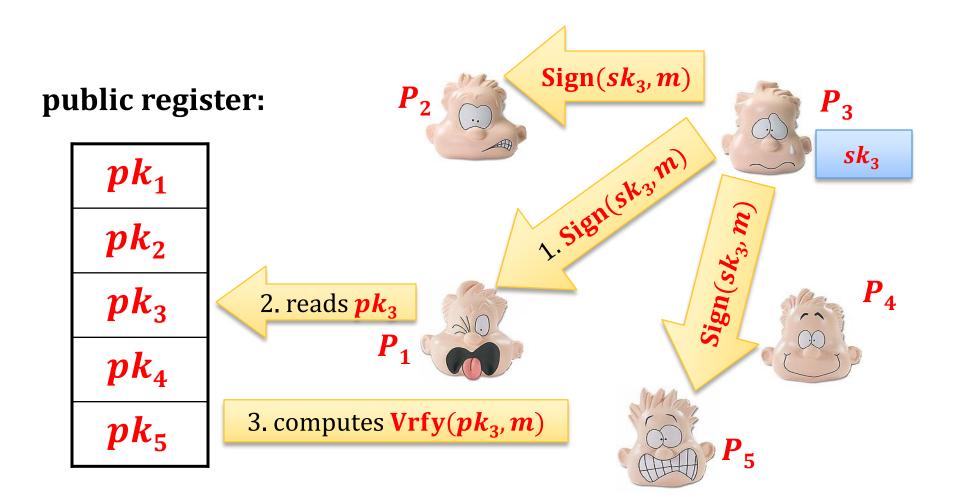
Sign – the signing algorithm



Anyone can send encrypted messages to anyone else



Anyone can verify the signatures



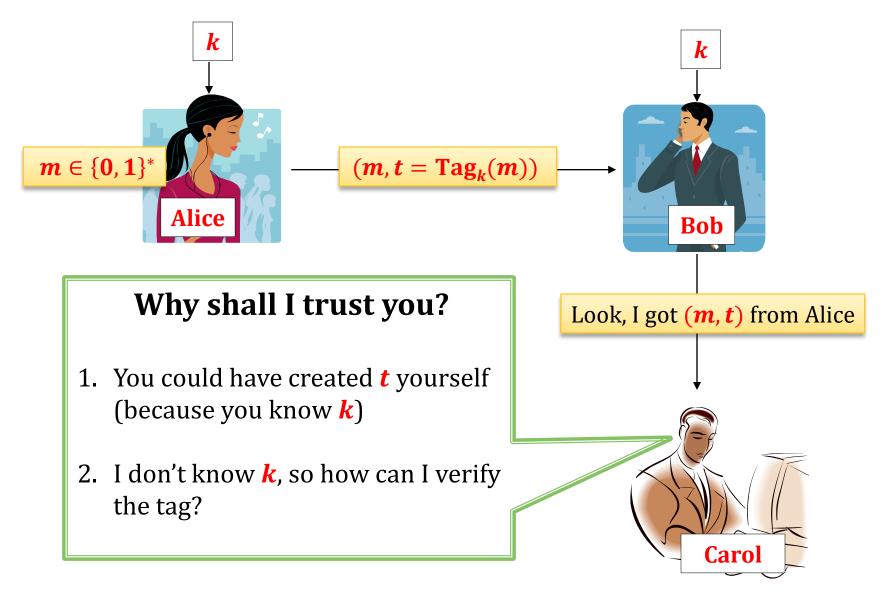
Advantages of the signature schemes

Digital signatures are:

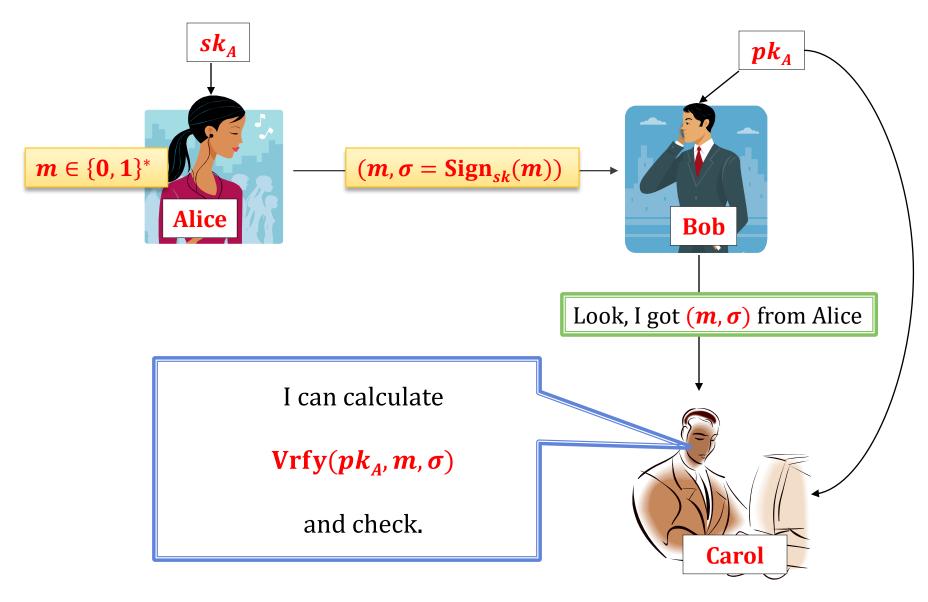
- 1. publicly verifiable,
- 2. transferable, and
- 3. provide **non-repudiation**

(we explain it on the next slides)

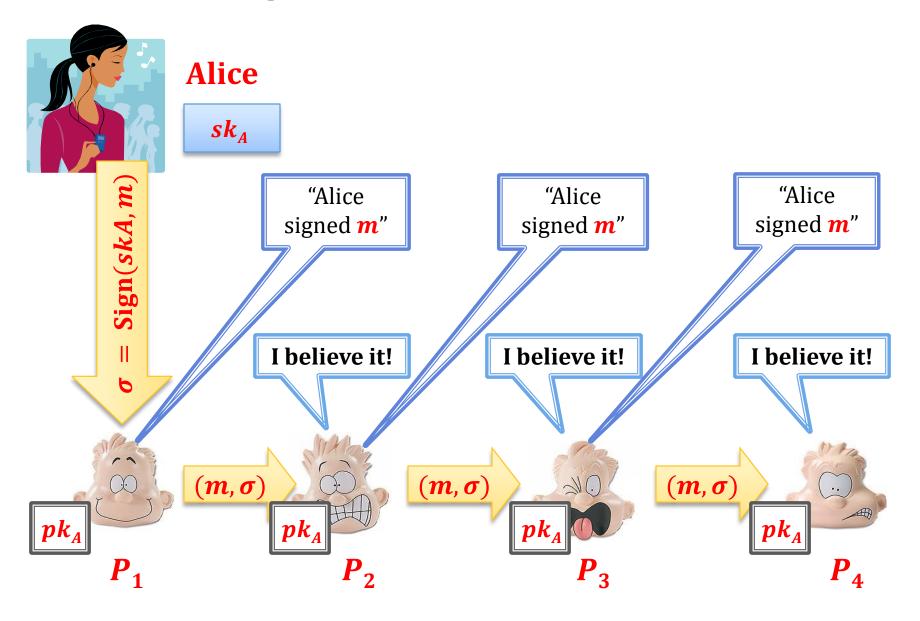
Look at the MACs...



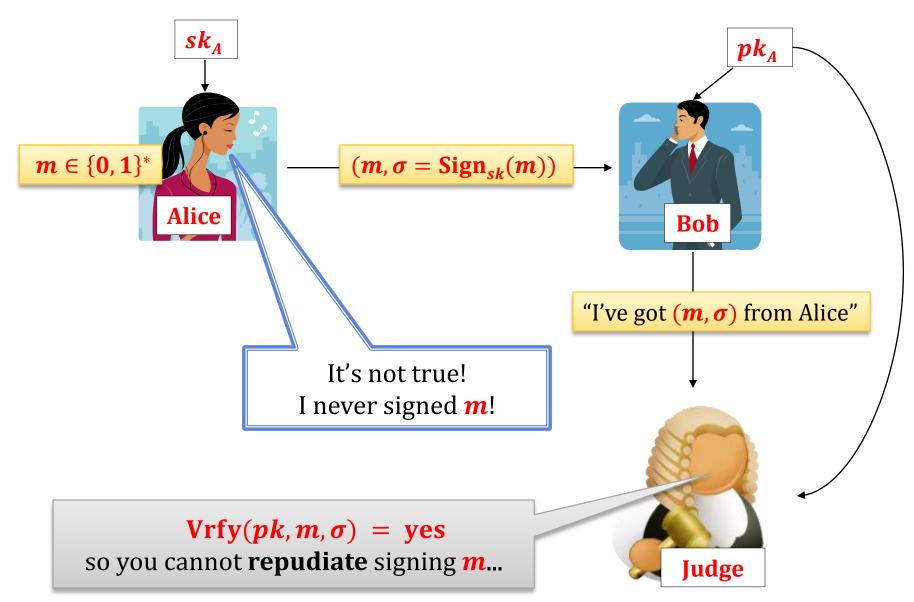
Signatures are publicly-verifiable!



So, the signatures are transferable



Non-repudiation



Things that need to be discussed

- Who maintains "the register"?
- How to contact it securely?
- How to **revoke the key** (if it is lost)?

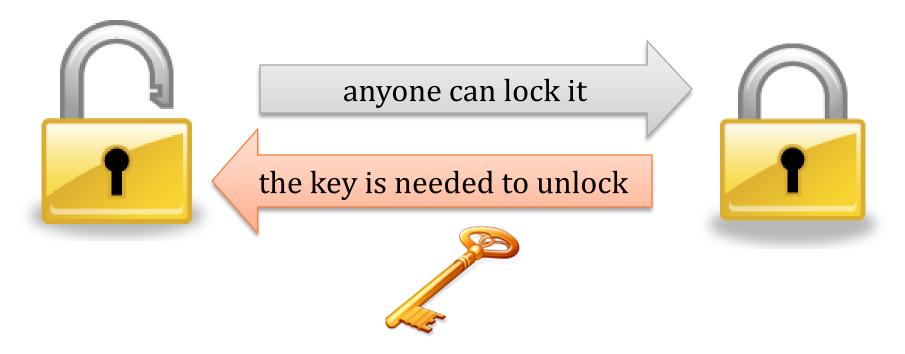
We will discuss these things later, when we will be talking about the **Public-Key Infrastructure**

But is it possible?

In the "physical world": **yes!**

Examples:

- 1. "normal" signatures
- 2. padlocks:



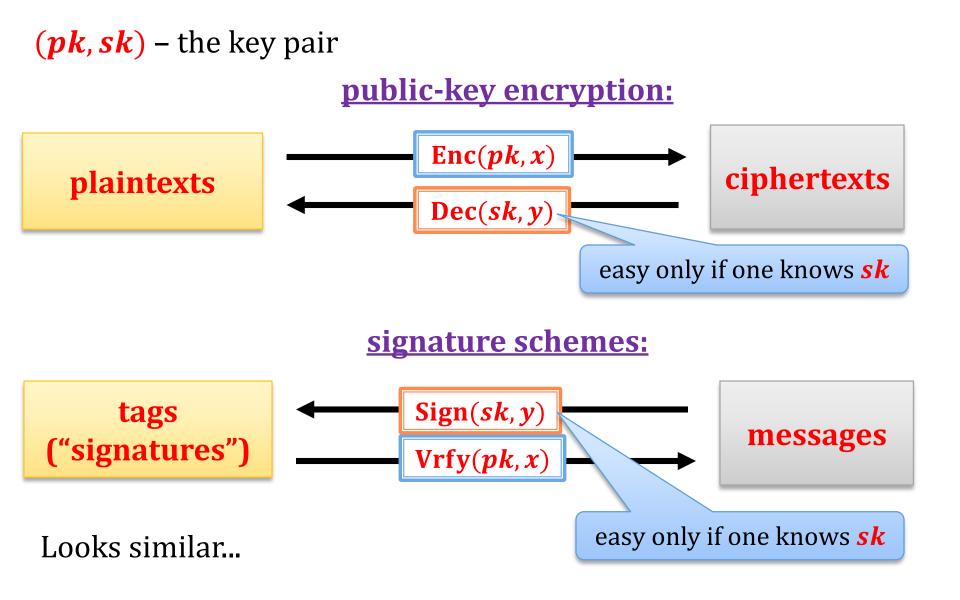
Diffie and Hellman (1976)

Diffie and Hellman proposed the public key cryptography in **1976**.

They just proposed the **concept**, not the **implementation**.

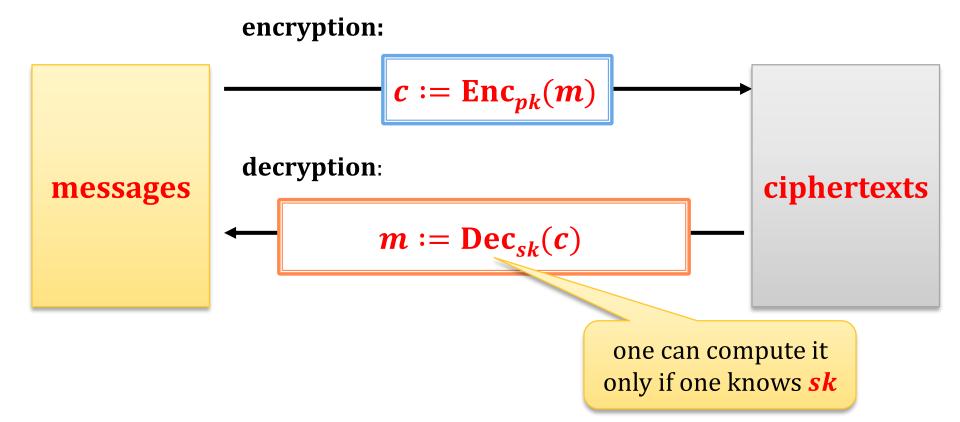
They have also shown a protocol for key-exchange.

The observation of Diffie and Hellman:



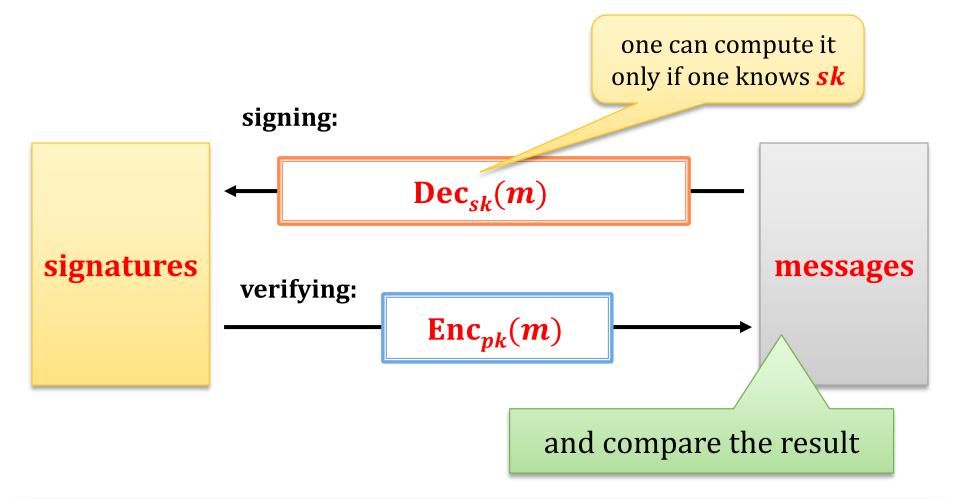
Trapdoor permutations (informal definition) A family of permutations indexed by $pk \in keys$: ${\operatorname{Enc}_{pk}: X \to X}_{pk \in \operatorname{keys}}$ such that for every key *pk* there exists a key *sk*, and: this is denoted Decsk **Enc**_{pk} easy X X • **easy**: one can compute Enc_{nk}^{-1} if one knows a **trapdoor** sk • hard (otherwise)

How to encrypt a message *m*



Warning: In reality it's not that simple. We will explain it later.

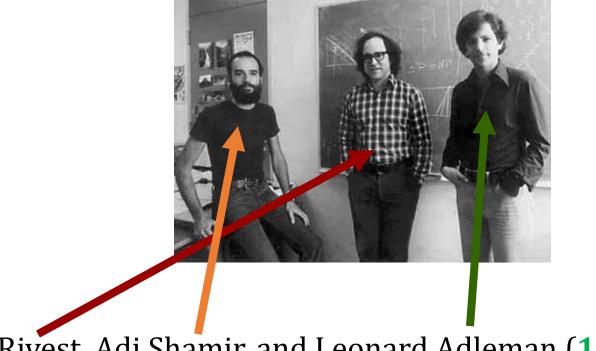
How to sign a message *m*



Warning: In reality it's not that simple. We will explain it later.

Do such functions exist?

Yes: exponentiation modulo *N*, where *N* is a product of two large primes.



Ron Rivest, Adi Shamir, and Leonard Adleman (1977)

RSA function is (conjectured to be) a trapdoor permutation!

The RSA function

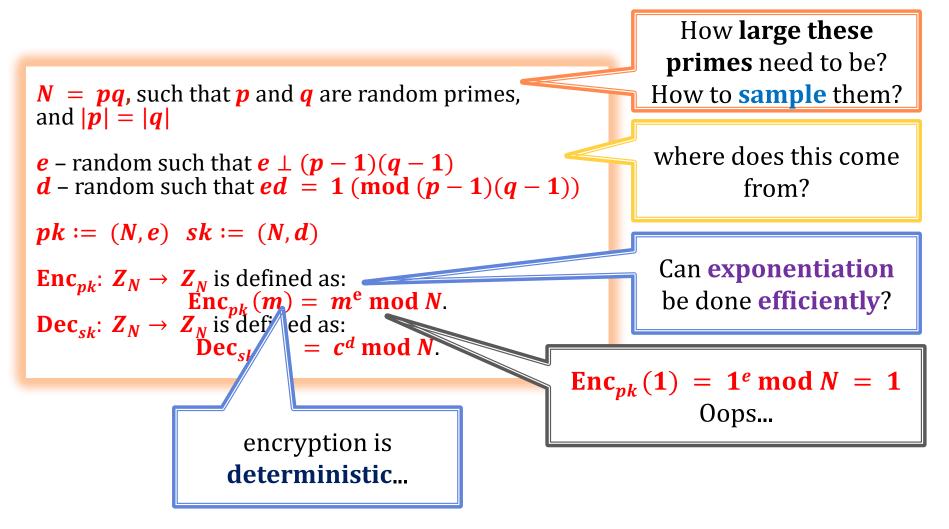
N = pq, such that p and q are random primes, and |p| = |q|

e - random such that $e \perp (p-1)(q-1)$ *d* - random such that $ed = 1 \pmod{(p-1)(q-1)}$

$$pk := (N, e) \quad sk := (N, d)$$

Enc_{pk}: $Z_N \rightarrow ZN$ is defined as: Enc_{pk} $(m) = m^e \mod N$. Dec_{sk}: $Z_N \rightarrow ZN$ is defined as: Dec_{sk} $(c) = c^d \mod N$.

Questions and doubts



We will address them later...

(*N*, *e*, *d*) – as on the previous slide

"Handbook" RSA

Handbook RSA encryption scheme:

messages and ciphertexts: Z_N

- $\operatorname{Enc}_{N,e}(m) = m^e \mod N$
- $\operatorname{Dec}_{N,d}(c) = c^d \mod N$

Handbook RSA signature scheme: messages and signatures: Z_N

- $\sigma \coloneqq \operatorname{Sign}_{N,d}(m) = m^d \mod N$
- $\operatorname{Vrfy}_{N,e}(m,\sigma) = \operatorname{output} \operatorname{yes} \operatorname{iff} \sigma^e \operatorname{mod} N = m$

Is **RSA** secure?

Is **RSA** secure:

- 1. as an **encryption scheme**?
- 2. as a **signature scheme**?

The answer is not that simple.

First, we would need to define security! We will do it on the next lectures.

Symmetric vs asymmetric crypto

Symmetric cryptography (also called: private key cryptography) is **much more efficient**!

Example (Intel Core 2 1.83 GHz processor):

	MiB/Second	Cycles/Byte
AES/CTR (128-bit key)	139	12.6
HMAC(SHA-1)	147	11.9

	Operations/Second	Megacycles/Operation
RSA 2048 Encryption	6,250	0.29
RSA 2048 Signature	165	11.06

Source: https://www.cryptopp.com/benchmarks.html

Practical solutions

Typically **asymmetric cryptography** is **combined** with the **symmetric one**.

For example: asymmetric cryptography is used only for **agreeing on a symmetric key**.

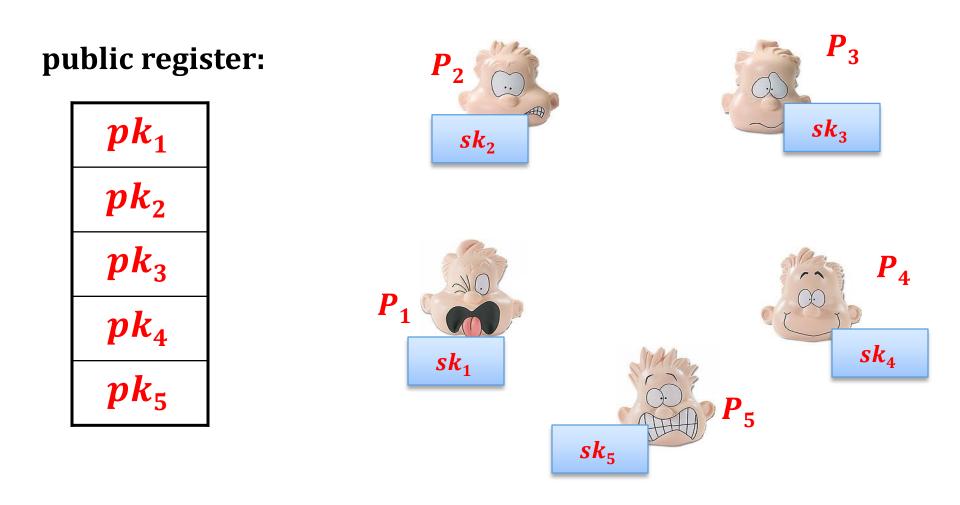
<u>Or</u>: one can combine it directly using a "**hybrid** approach".

(we will discuss it later)

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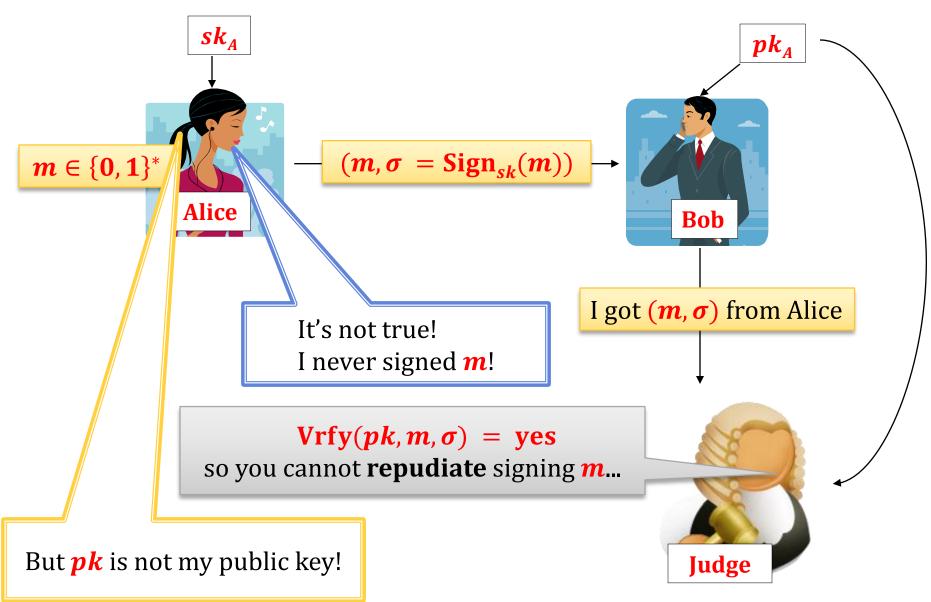
Remember this slide?



Question: How to maintain the public register?

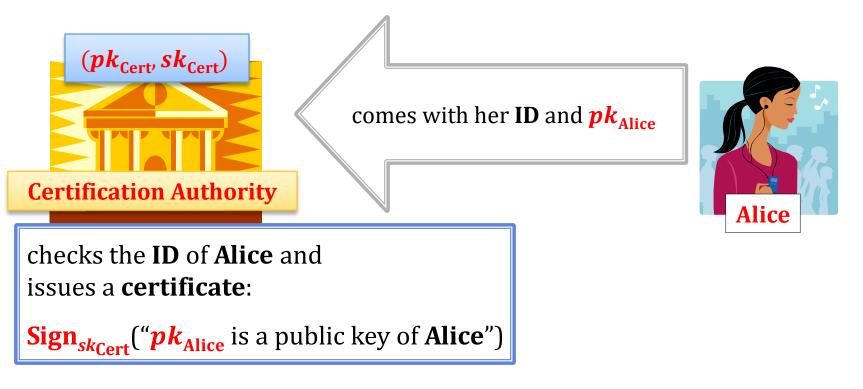
- 1. We start with the case when the public keys are used for **signing that is legally binding**.
- 2. Then we consider other cases.

A problem



Solution: certification authorities

A simplified view:



Now, **everyone** can verify that pk_{Alice} is a public key of **Alice**. So **Alice** can attach it to every signature really everyone?

What is needed to verify the certificate

To verify the certificate coming from **Cert** one needs:

- 1. to **know** the public key of the **Cert**
- 2. to **trust Cert**.

It is better if **Cert** also keeps a document: *"I, Alice certify that pk_{Alice} is my public key"* with a **written** signature of **Alice**.

How does it look from the legal point of view?

What matters at the end is if you can **convince the judge**.

Many countries have now a special law regulating these things.

In **Poland**:

Ustawa o podpisie elektronicznym, z dnia 18 września 2001 r. (Dz.U.01.130.1450) 28 str. (<u>ISIP</u>), na podst. dyrektywy EU <u>1999/93/EC</u> This law defines the conditions to become an official **certification authority**.

A certificate issued by such an authority is called a **qualified certificate**.

A signature obtained this way is called a **qualified digital signature**.

The **qualified signature** is equivalent to the written one!

Polish Certificate Authorities:

NCCERT NBP	ENGLISH ARCHIWUM KONTAKT			UM KONTAKT
NBP Narodowy Bank Polski	Narodowe C	Narodowe Centrum Certyfikacji (NCCert)		
Strona główna Dokumenty Podmioty kwalifiko	wane Zaświadczenia certyfikacyjne	Lista CRL	Lista TSL	Komunikaty
				2015
				2013
REJECTR KWALTERKOWANYOU RORMATÓW				2012
REJESTR KWALIFIKOWANYCH PODMIOTÓW			2011	
ŚWIADCZĄCYCH USŁUGI CERTYFIKACYJNE				2010
				2009
Narodowy Bank Polski prowadzi rejestr podmiotów kwalifikowanych od dnia 1 października 2005r.				2007
				2006
Plik: NCCert.crt - zaświadczenie certyfikacyjne Narodowego C	atrum Certyfikacji - (nowy root)			2005

Wpisy uszeregowane pod kątem czasu uzyskania wpisu do rejestru - w kolejności od najwcześniejszego

Numer wpisu	Nazwa podmiotu	Rodzaj świadczonych usług	Czas dokonania wpisu
1.	UNIZETO TECHNOLOGIES	Wydawanie kwalifikowanych certyfikatów	31 grudnia 2002 r.,godz. 12:00:00
	Spółka Akcyjna	Wydawanie kwalifikowanych certyfikatów atrybutów	13 września 2007 r.,godz. 10:00:00
		Znakowanie czasem	24 stycznia 2003 r., godz. 12:00:00

So, what to do if you want to issue the qualified signatures?

You have to go to one of these companies and **get a qualified certificate** (it costs!).

The certificate is **valid just for some period**.

What if the secret key is lost?

In this case you have to **revoke** the certificate.

Every authority maintains a list of **revoked certificates**.

The certificates come with some insurance.

In many case one doesn't want to use the qualified signatures

The certificates cost.

It's **risky** to use them:

How do you know what your computer is really signing? Computers have **viruses, Trojan horses**, etc.

You can use **external trusted hardware** but it should have a display (so you can see what is signed).

Remember: qualified signatures are equivalent to the written ones!

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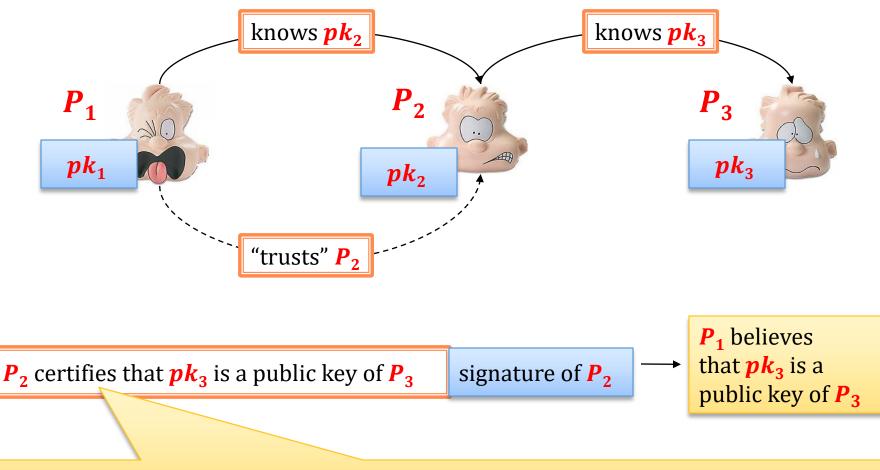
Practical solution

In many cases the **qualified signatures** are an overkill.

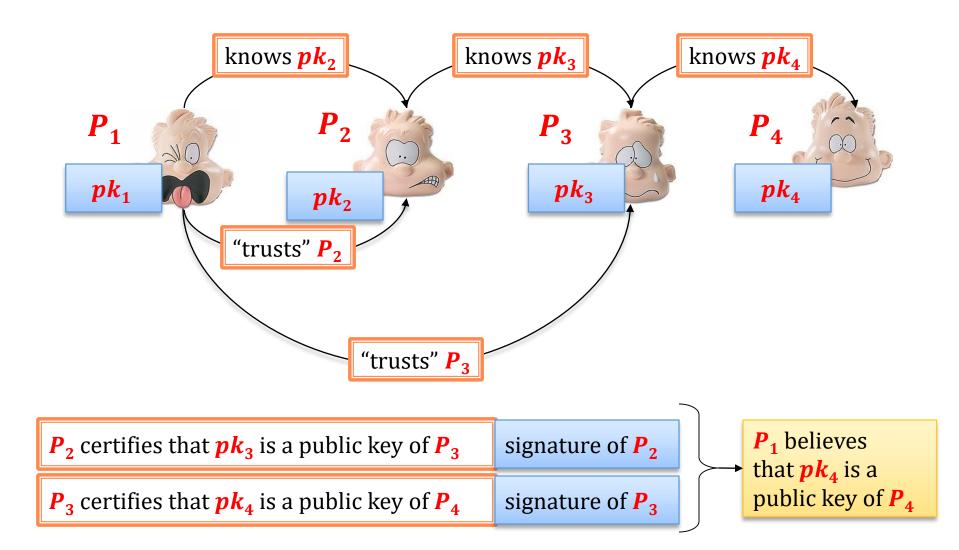
Instead, people use **non**-qualified signatures.

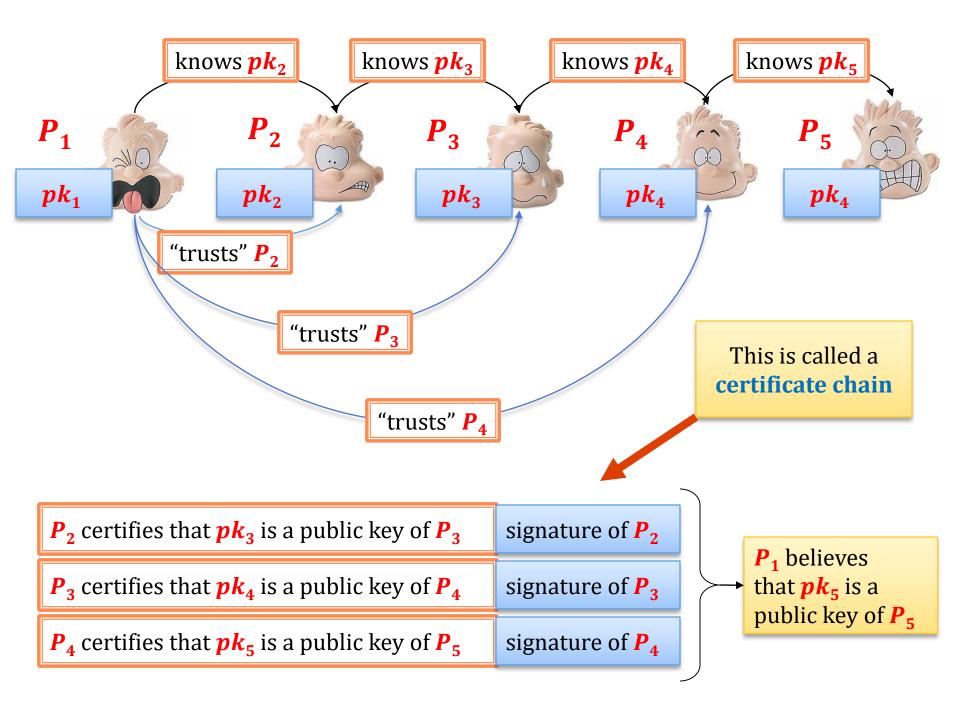
The certificates are distributed using a **public-key infrastructure (PKI)**.

Users can certify keys of the other users

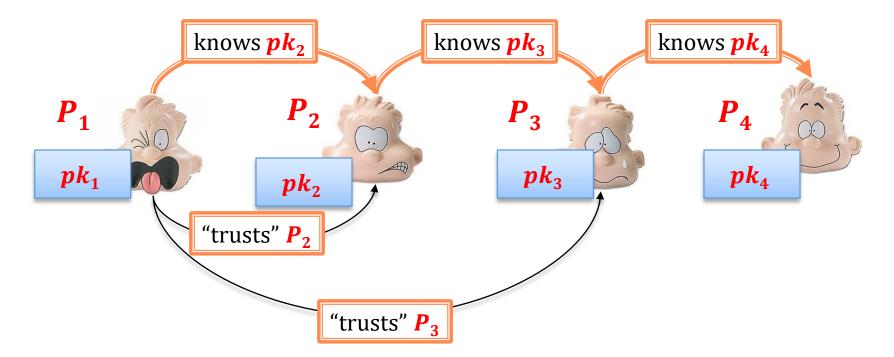


this should be done only if P_2 really met P_3 in person and verified his identity





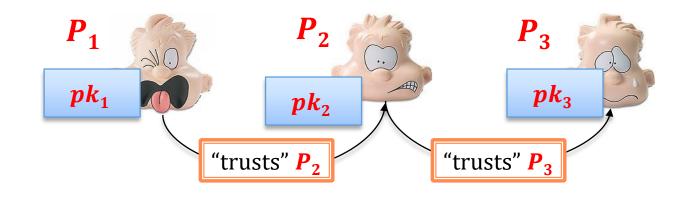
A problem



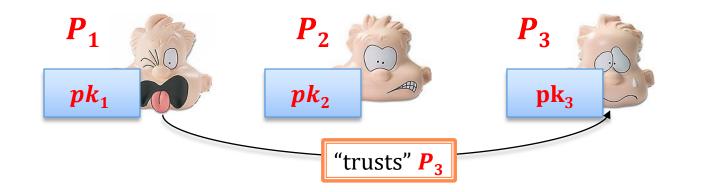
What if P_1 does not know P_3 ? How can he trust him? Answer: P_2 can recommend P_3 to P_1 .

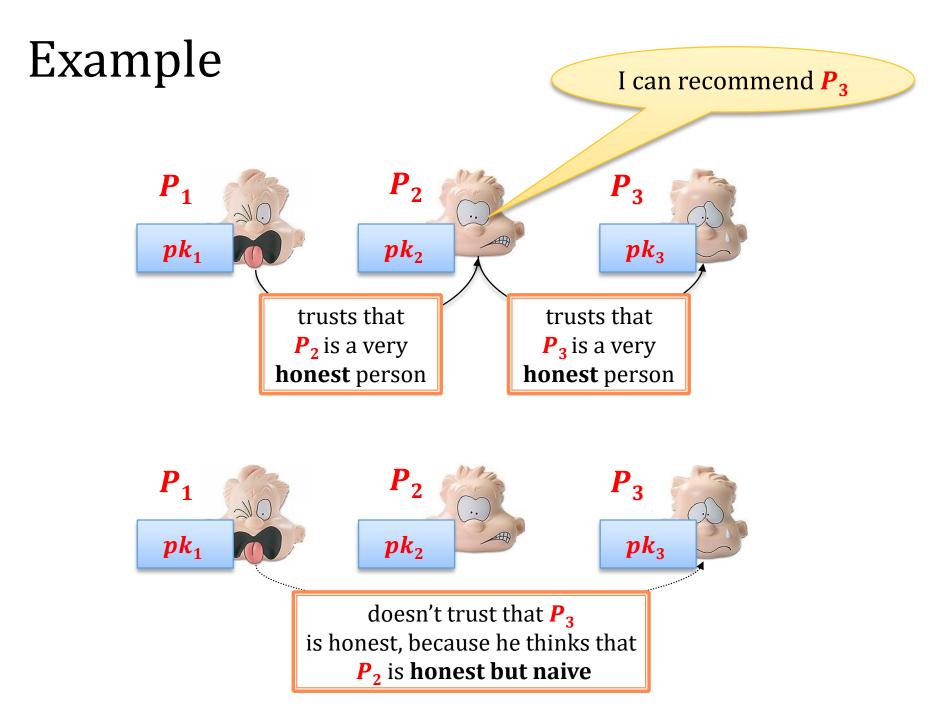
A question: is trust transitive?





imply:







Trust is not transitive:

"*P*₁ trusts in the certificates issued by *P*₂"

is not the same as:

"P₁ trusts that if P₂ says: "you can trust the certificates issued by P₃" then one can trust the certificates issued by P₃"

Recommendation levels

level 1 recommendation:
 A: "you can trusts in all the certificates issued by B"

level 2 recommendation: A : "you can trust that all the level 1 recommendations issued by B"

level 3 recommendation: A : "you can trust that all the level 2 recommendations issued by B"

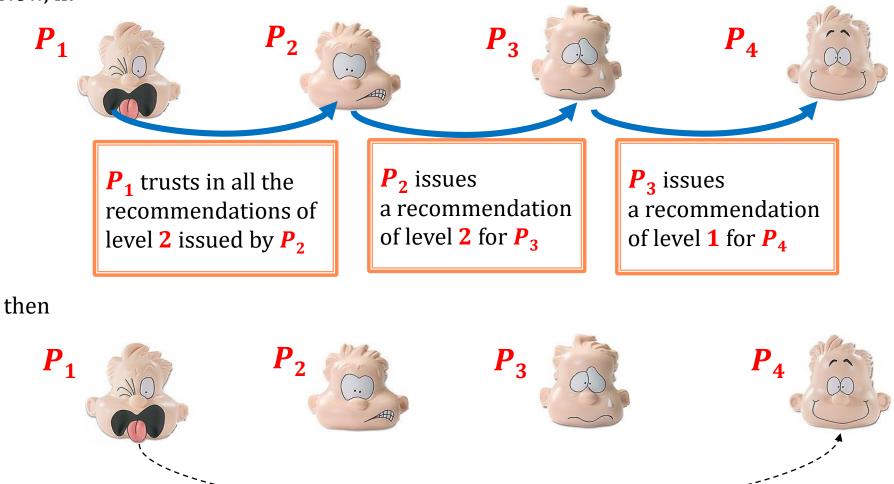
and so on...

<u>Recursively</u>:

level i + 1 recommendation:

A : "you can trust that all **the level** i recommendations issued by B"

Now, if:



trusts the certificates issued by P_4

Of course the recommendations also need to be signed.

Starts to look complicated...

How is it solved in practice?

In popular standard is **X.509** the recommendation is included into a certificate.

Here the level of recommendations is bounded using a field called *basic constraints*.

X.509 is used for example in **SSL**.

SSL is implemented is implemented in every popular web-browser.

So, let's look at it.

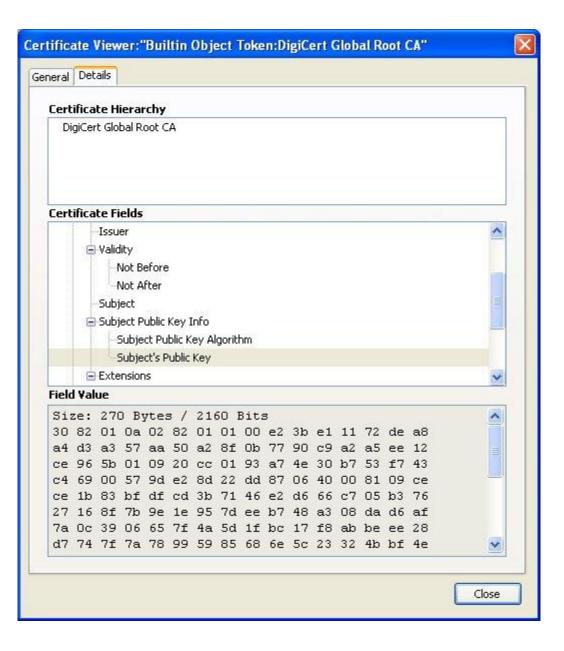
🥹 Certificate Manager



Certificate Name	Security Device	E,
Baltimore CyberTrust Root	Builtin Object Token	~
🖃 Certplus		
-Class 2 Primary CA	Builtin Object Token	
🖃 Comodo CA Limited		_
-AAA Certificate Services	Builtin Object Token	
-Secure Certificate Services	Builtin Object Token	
-Trusted Certificate Services	Builtin Object Token	
🖃 DigiCert Inc		
-DigiCert Assured ID Root CA	Builtin Object Token	
DigiCert Global Root CA	Builtin Object Token	
-DigiCert High Assurance EV Root CA	Builtin Object Token	
🖃 Digital Signature Trust		
DST ACES CA X6	Builtin Object Token	
🖃 Digital Signature Trust Co.		
- Digital Signature Trust Co. Global CA 1	Builtin Object Token	
Digital Signature Trust Co. Global CA 3	Builtin Obiect Token	×
View Edit Import	Delete	

Certificate Viewer: "Builtin Object Token: DigiCert Global Root CA" × General Details This certificate has been verified for the following uses: Email Signer Certificate SSL Certificate Authority Status Responder Certificate Issued To DigiCert Global Root CA Common Name (CN) Organization (O) DigiCert Inc Organizational Unit (OU) www.digicert.com Serial Number 08:3B:E0:56:90:42:46:B1:A1:75:6A:C9:59:91:C7:4A **Issued By** Common Name (CN) DigiCert Global Root CA Organization (O) DigiCert Inc Organizational Unit (OU) www.digicert.com Validity Issued On 11/10/2006 Expires On 11/10/2031 Fingerprints SHA1 Fingerprint A8:98:5D:3A:65:E5:E5:C4:B2:D7:D6:6D:40:C6:DD:2F:B1:9C:54:36 MD5 Fingerprint 79:E4:A9:84:0D:7D:3A:96:D7:C0:4F:E2:43:4C:89:2E Close

Certificate Hierarchy	
DigiCert Global Root CA	
ertificate Fields	
-Subject Public Key Algorithm	~
Subject's Public Key	
Extensions	
- Certificate Key Usage	
- Certificate Basic Constraints	-
-Certificate Subject Key ID	
Certificate Authority Key Identifier	
Certificate Signature Algorithm	
Certificate Signature Value	~
ïeld Value	
PKCS #1 SHA-1 With RSA Encryption	

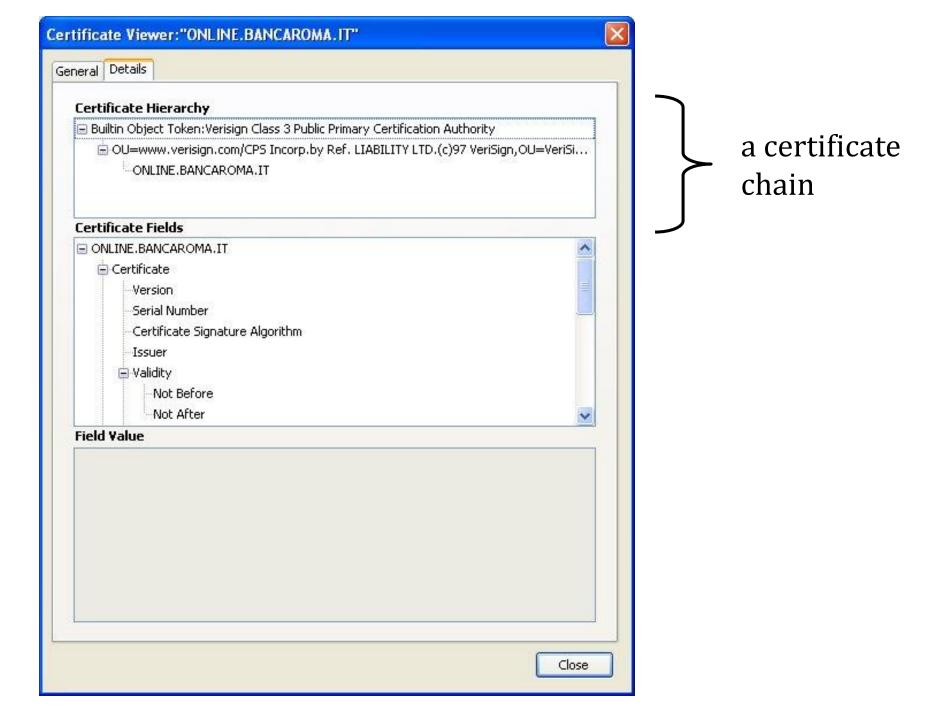


Certificate Hierarchy DigiCert Global Root CA	
DigiCert Global Root CA	
Certificate Fields	
Not After	
-Subject	
Subject Public Key Info Subject Public Key Algorithm	
-Subject's Public Key	
Extensions	
-Certificate Key Usage	
Certificate Basic Constraints	
Certificate Subject Key ID	this field limits the
Field ¥alue	
Critical	recommendation
Is a Certificate Authority	
Maximum number of intermediate CAs: unlimited	depth
	(here it's unlimited)
	(nere it s'unimiteu)
Close	

Concrete example

Let's go to the Banca Di Roma website

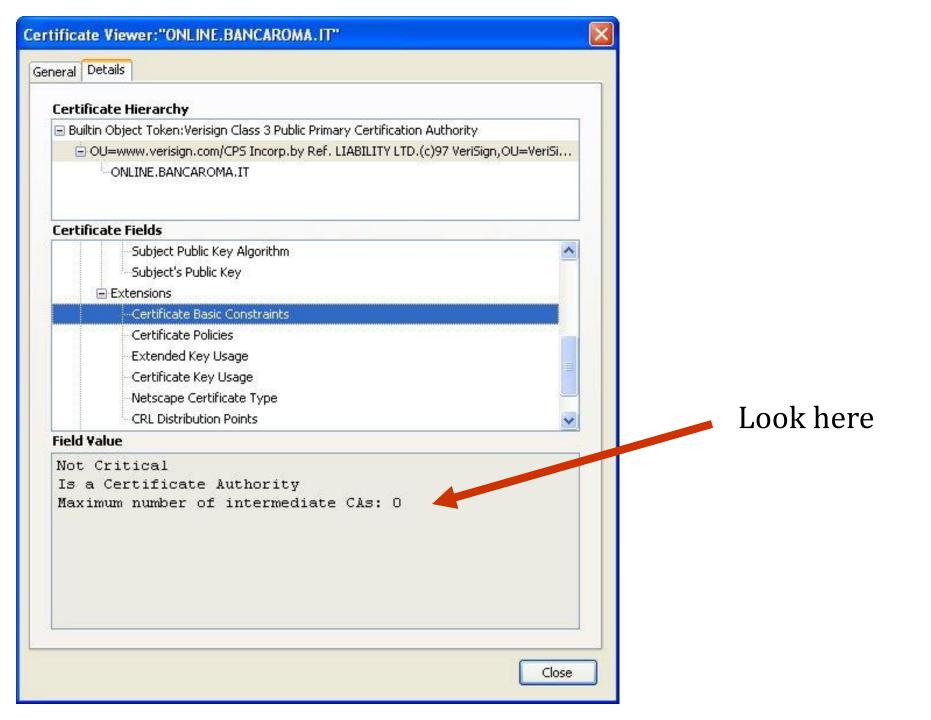
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ertifical	e Hierarchy
Builtin C	bject Token:Verisign Class 3 Public Primary Certification Authority
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L.	ONLINE.BANCAROMA.IT
ertifical	e Fields
	w.verisign.com/CPS Incorp.by Ref. LIABILITY LTD.(c)97 VeriSign,OU=VeriSi 🔼
1 13	ificate
- 10 E	Version
- 13 E	Serial Number
	Certificate Signature Algorithm
	Issuer
	Validity
	-Not Before
	Not After
eld Valu	e
OU = C	lass 3 Public Primary Certification Authority riSign, Inc.

the second certificate was signed by **"Verisign Primary Authority"** for **"Verisign Inc".**

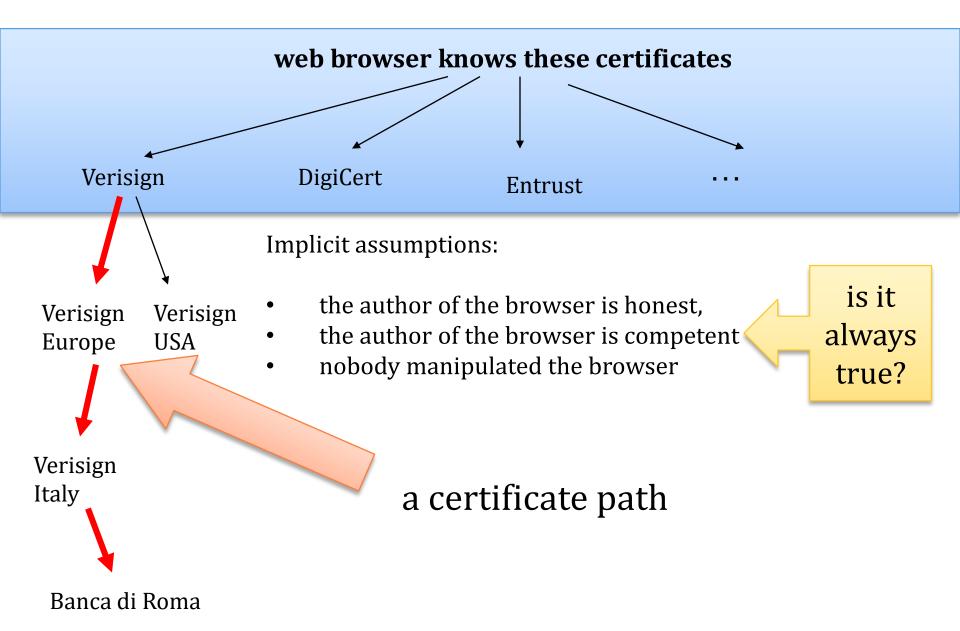
(it's not strange, we will discuss it)

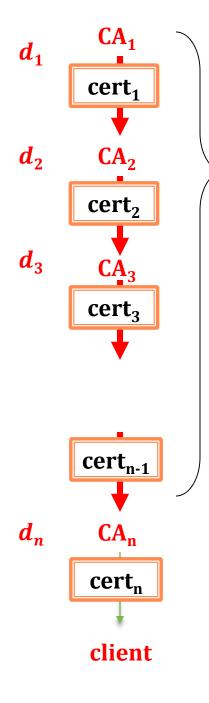


ertificat	e Hierarchy
	bject Token:Verisign Class 3 Public Primary Certification Authority
1.1	=www.verisign.com/CPS Incorp.by Ref. LIABILITY LTD.(c)97 VeriSign,OU=VeriSi
	ONLINE,BANCAROMA,IT
Ertificat	e Fields
	Subject Public Key Algorithm
	¹ Subject's Public Key
	Extensions
	Certificate Basic Constraints
	Certificate Key Usage
	CRL Distribution Points
	Certificate Policies
	Extended Key Usage
ield Valu	Authority Information Access
	itical a Certificate Authority
15 1100	a cercificate wathority

The third certificate was issued by **Verisign Inc.** for **Banca di Roma**

The typical picture





All these certificates have to have a flag **"Is a Certification Authority"** switched on.

Moreover:

each **cert**_i has a number **d**_i denoting a maximal depth of certificate chain from this point (this limits the recommendation depth)

That is, we need to have: $d_i \ge n - i$

Is it so important to check it?

Yes!

For example: the last element in the chain can be anybody (who paid to **Verising** for a certificate).

For sure we do not want to trust the certificates issued by **anyone**.

So, what happens when a user contacts the bank?



If Alice's browser knows $cert_1$ it can verify the chain and read the public key of the bank from $cert_n$.

Other information that the certificats contain

- information about the signature algorithm
- validity (dates)
- address of the **certificate revocation list**

Certificate Revocation List (CRL): the list of revoked certificates (need to access it before accepting the certificate)

Main problems with X.509

- **1. Certificate revocation lists** work only **if you are online**.
- 2. Revocation of root certificates not addressed.
- **3. CAs cannot restrict the domains** on which the subordinate CAs issue certificates.
- 4. It's enough into hack one of the popular CA's to impersonate any webpage.

Not only theoretical problems

DigiNotar SSL certificate hack amounts to cyberwar, says expert

Google slaps Symantec for issuing fake web security certificates

transactions, se than

by Jon Fingas | @jonfingas | October 29th 2015 At 8:22pm



Share this article: 📑 😏 in 👷 🗔

A Turkish certificate authority (CA) accidentally issued two intermediate, or chained, digital certificates, one of which was used by the holder to mimic legitimate websites.

A solution: "Public Key Pinning":

- after the first connection the web browser remembers the public keys on the certificate chain,
- in each subsequent connection the browser **checks if the certificate chain is the same** as before.

Another problem

In practice:

the certificate **issuers do not check the identity** of their customers carefully

(due to the economical reasons).

Solution: Extended Validation Certificates

Some certificates are issued after **a more careful check**. This is indicated in the web browser.

Example from Chrome:

EV certificate:

← → C G Credit Agricole Bank Polska S.A. [PL] https://e-bank.credit-agricole.pl

Non-EV certificate:

← → C https://usosweb.mimuw.edu.pl/

A different idea for a PKI

Namecoin

use Bitcoin's "blockchain" as a distributed register.

Another popular PKI (in the past)

Pretty Good Privacy (PGP) – every user can act as a certification authority.

Hence the name:

Web of Trust

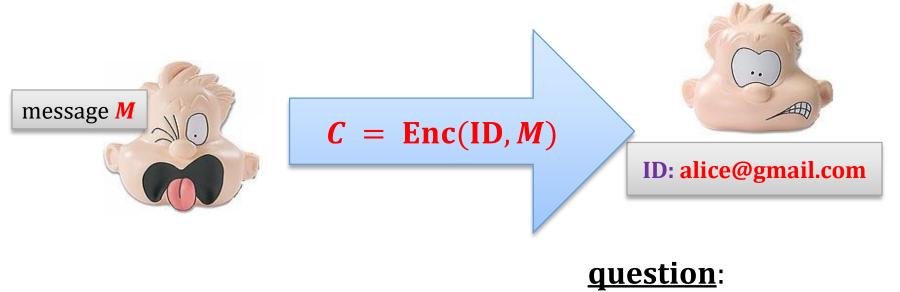
Plan

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Identity based cryptography

<u>Main idea</u>:

the identifier **ID** of the user is its public key. (e.g. **ID** = user's email address).

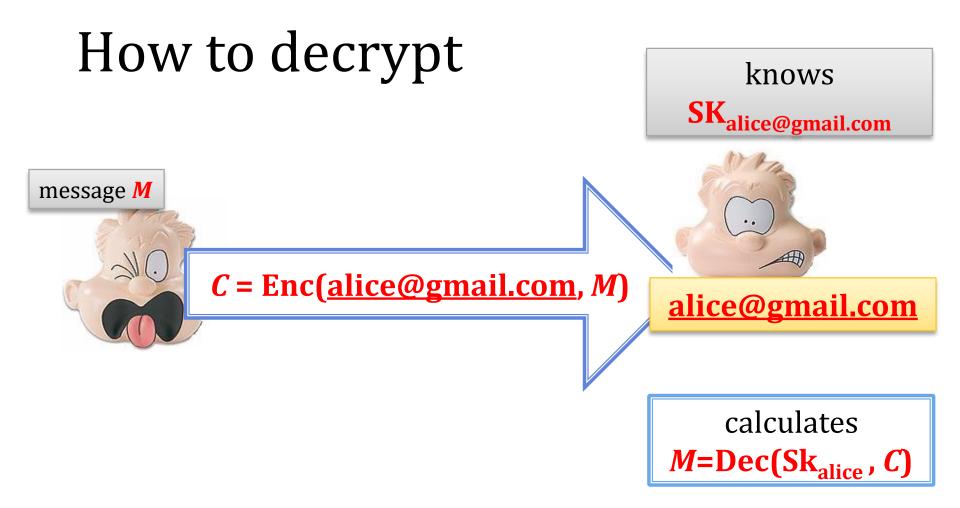


What is the private key?

Solution



sent over a secure link



ID-based encryption

Main **advantage**:

no need for an "infrastructure"

Drawbacks:

- users need to **trust an authority**,
- and they need to have a **secure link** to it,
- what about the **key revocation**?

ID-based encrypion

Proposed by **Adi Shamir** in **1984**. (he only implemented the identity-based <u>signatures</u>)

First schemes were proposed by **Boneh** and **Franklin** (2001) and, independently **Cocks** (2001).

In **2002 Boneh** started a company

Voltage Security

that produces solutions based on his ID-based scheme.

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